

# Trade Costs

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## Introduction

Trade costs are the costs a trader must pay to implement a decision to buy or sell a security. Consider a single trade of a single equity security. Suppose on the evening of August 1, a trader decides to purchase 10,000 shares of IBM at \$10, the *decision price* of the trade. The next day, the trader's broker buys 10,000 shares in a rising market and pays \$11 per share, the trade's *execution price*.

How much did it cost to implement this trade? In the most basic ex-post analysis, trade costs are calculated by comparing the execution price of a trade to a benchmark price.<sup>1</sup> Suppose we wished to compare the execution price to the price of the security at the time of the decision in the above example. Since the trader's decision occurred at \$10 and the broker paid \$11, the cost of the trade relative to the decision price was  $\$11 - \$10 = \$1$  per share, or \$10,000 (9.1% of the total value of the execution).

Measuring costs relative to a trade's decision price captures costs associated with the delay in the release of a trade into the market and movements in price after the decision was made but before the order is completed. It does not, however, provide a means to determine whether the broker's execution reflects a fair price. For example, the price of \$11 would be a poor price if most transactions in IBM on August 2 occurred at \$10.50. For this purpose a better benchmark would be the day's volume-weighted average price, or VWAP. If VWAP on August 2 was \$10.50 and the trader used this as her benchmark, then the trade cost would be \$0.50 per share, or \$500.

The first version of the **tradeCosts** package provides a simple framework for calculating the cost of trades relative to a benchmark price, such as VWAP or decision price, over multiple periods and basic reporting and plotting facilities to analyse these costs.

## Trade costs in a single period

Suppose we want to calculate trade costs for a single period. First, the data required to run the analysis must be assembled into three data frames. A sample of each of the three types of data has been included with the package in three data sets.

The first data frame contains all trade-specific information, a sample of which is in the `trade.mar.2007` data frame:

```
> library(tradeCosts)
```

```
> data(trade.mar.2007)
> head(trade.mar.2007)
```

	period	id	side	exec.qty	exec.price
1	2007-03-01	03818830	X	60600	1.60
2	2007-03-01	13959410	B	4400	32.21
3	2007-03-01	15976510	X	13600	7.19
4	2007-03-01	22122P10	X	119000	5.69
5	2007-03-01	25383010	X	9200	2.49
6	2007-03-01	32084110	B	3400	22.77

Trading data must include at least the set of columns included in the sample shown above: `period` is the period during which the trade was executed, in this case a calendar trade day; `id` is a unique security identifier; `side` must be one of B (buy), S (sell), C (cover) or X (short sell); `exec.qty` is the number of shares executed; and `exec.price` is the price per share of the execution.

Second, trade cost analysis requires dynamic descriptive data, or data that changes across periods for each security.

```
> data(dynamic.mar.2007)
> head(dynamic.mar.2007[c("period", "id", "vwap",
+ "prior.close")])
```

	period	id	vwap	prior.close
1	2007-03-01	00797520	3.88	3.34
2	2007-03-01	010015	129.35	2.53
3	2007-03-01	023282	613.57	12.02
4	2007-03-01	03818830	1.58	1.62
5	2007-03-01	047628	285.67	5.61
6	2007-03-01	091139	418.48	8.22

The `period` and `id` columns match those in the trading data. The remaining two columns in the sample are benchmark prices: `vwap` is the volume-weighted average price for the period and `prior.close` is the security's prior period closing price.

The final data frame contains static data for each security.

```
> data(static.mar.2007)
> head(static.mar.2007)
```

	id	symbol	name	sector
1301	00036020	AAON	Aaon Inc	IND
2679	00036110	AIR	Aar Corp	IND
3862	00040010	ABCB	Ameris Bancorp	FIN
406	00080S10	ABXA	Abx Air Inc	IND
3239	00081T10	ABD	Acco Brands Corp	IND
325	00083310	ACA	Aca Capital Hldgs Inc -redh	FIN

The `id` column specifies an identifier that can be linked to the other data frames. Because this data is static, there is no `period` column.

Once assembled, these three data frames can be analysed by the `trade.costs` function:

<sup>1</sup>For an in-depth discussion of both ex-ante modeling and ex-post measurement of trade costs, see Kissell and Glantz (2003).

```
> result <- trade.costs(trade = trade.mar.2007,
+   dynamic = dynamic.mar.2007,
+   static = static.mar.2007,
+   start.period = as.Date("2007-03-01"),
+   end.period = as.Date("2007-03-01"),
+   benchmark.price = "vwap")
```

The `trade`, `dynamic`, and `static` arguments refer to the three data frames discussed above. `start.period` and `end.period` specify the period range to analyse. This example analyses only one period, March 1, 2007, and uses the `vwap` column of the `dynamic` data frame as the benchmark price. `result` is an object of class `tradeCostsResults`, upon which we can call the `summary` method:

```
> summary(result)
```

Trade Cost Analysis

Benchmark Price: vwap

Summary statistics:

Total Market Value:	1,283,963
First Period:	2007-03-01
Last Period:	2007-03-01
Total Cost:	-6,491
Total Cost (bps):	-51

Best and worst batches over all periods:

	batch.name	exec.qty	cost
1	22122P10 (2007-03-01 - 2007-03-01)	119,000	-3,572
2	03818830 (2007-03-01 - 2007-03-01)	60,600	-1,615
3	88362320 (2007-03-01 - 2007-03-01)	31,400	-1,235
6	25383010 (2007-03-01 - 2007-03-01)	9,200	33
7	13959410 (2007-03-01 - 2007-03-01)	4,400	221
8	32084110 (2007-03-01 - 2007-03-01)	3,400	370

Best and worst securities over all periods:

	id	exec.qty	cost
1	22122P10	119,000	-3,572
2	03818830	60,600	-1,615
3	88362320	31,400	-1,235
6	25383010	9,200	33
7	13959410	4,400	221
8	32084110	3,400	370

NA report:

	count
id	0
period	0
side	1
exec.price	0
exec.qty	0
vwap	0

The first section of the report above provides high-level summary information. The total unsigned market value of trades for March 1 was around \$1.3mm. Relative to VWAP, these trades cost -\$6,491, indicating that overall the trades were executed at a level better than VWAP. This total cost is the sum of the signed cost of each trade relative to the benchmark price. As a percentage of total executed market value, this set of trades cost -51 bps less than VWAP.

The next section displays the best and worst *batches* over all periods. We will discuss batches in the next section. For now, note that when dealing with only one period, each trade falls into its own

batch, so this section shows the most and least expensive trades for March 1. The next section displays the best and worst securities by total cost across all periods. Because there is only one trade per security on March 1, these results match the best and worst batches by cost.

Calculating the cost of a trade requires a non-NA value for `id`, `period`, `side`, `exec.price` and `exec.qty`. The final section shows a count for each type of NA in the input data. Rows in the input data with NA's in any of these columns are removed before the analysis is performed and reported here.

## Costs over multiple periods

Calculating trade costs over multiple periods works similarly. Cost can be calculated for each trade relative to a benchmark price which is either specific to the period of the trade or fixed at the decision price.

Suppose, for example, that the trader decided to short a stock on a particular day, but he wanted to trade so many shares that it took several days to complete the order. For instance, consider the following sequence of trades in our sample data set for Progressive Gaming, PGIC, which has `id` 59862K10:

```
> subset(trade.mar.2007, id %in% "59862K10")
```

	period	id	side	exec.qty	exec.price
166	2007-03-13	59862K10	X	31700	5.77
184	2007-03-15	59862K10	X	45100	5.28
218	2007-03-19	59862K10	X	135800	5.05
259	2007-03-20	59862K10	X	22600	5.08

How should the trader calculate the cost of these trades? One way is to calculate the cost for each trade separately relative to a benchmark price such as `vwap`, exactly as in the last example. In this case, the cost of each trade in PGIC would be calculated relative to VWAP in each period and then added together. However, this method would ignore the cost associated with spreading out the sale over several days. If the price of the stock had been falling over the four days of the sale, as it appears to in this example, successive trades appear less attractive when compared to the price at the time of the decision. The trader can capture this cost by grouping the four short sales into a *batch* and comparing the execution price of each trade to the batch's original decision price.

Performing this type of multi-period analysis using `tradeCosts` requires several modifications to the previous single period example. Note that since no period range is given, analysis is performed over the entire data set:

```
> result.batched <- trade.costs(trade.mar.2007,
+   dynamic = dynamic.mar.2007,
+   static = static.mar.2007,
+   batch.method = "same.sided",
+   benchmark.price = "decision.price")
```

First, `trade.costs` must be instructed how to group trades into batches by setting the `batch.method` parameter. This version of **tradeCosts** provides a single multi-period sample batch method, `same.sided`, which groups all consecutive same-sided orders into a single batch. Provided there were no buys in between the four sales in PGIC, all four trades would be grouped into the same batch. Second, setting `benchmark.price` to `decision.price` sets the benchmark price to the prior closing price of the first trade in the batch. Running summary on the new result yields the following:

```
> summary(result.batched)
```

Trade Cost Analysis

Benchmark Price: `decision.price`

Summary statistics:

Total Market Value:	47,928,402
First Period:	2007-03-01
Last Period:	2007-03-30
Total Cost:	587,148
Total Cost (bps):	123

Best and worst batches over all periods:

	batch.name	exec.qty	cost
1	04743910 (2007-03-19 - 2007-03-19)	17,800	-82,491
2	31659U30 (2007-03-09 - 2007-03-13)	39,800	-33,910
3	45885A30 (2007-03-13 - 2007-03-19)	152,933	-31,904
274	49330810 (2007-03-13 - 2007-03-30)	83,533	56,598
275	15649210 (2007-03-15 - 2007-03-28)	96,900	71,805
276	59862K10 (2007-03-13 - 2007-03-20)	235,200	182,707

Best and worst securities over all periods:

	id	exec.qty	cost
1	04743910	17,800	-82,491
2	31659U30	51,400	-32,616
3	45885A30	152,933	-31,904
251	49330810	83,533	56,598
252	15649210	118,100	73,559
253	59862K10	235,200	182,707

NA report:

	count
id	0
period	0
side	4
exec.price	0
exec.qty	0
prior.close	0

This analysis covers almost \$50mm of executions from March 1 to March 30, 2007. Relative to decision price, the trades cost \$587,148, or 1.23% of the total executed market value.

The most expensive batch in the result contained the four sells in PGIC (59862K10) from March 13 to March 20, which cost \$182,707. Below is a list of each trade and its associated cost that contributed to this batch's total cost.

	period	id	side	exec.qty	exec.price
239	2007-03-13	59862K10	X	31700	5.77
240	2007-03-15	59862K10	X	45100	5.28
241	2007-03-19	59862K10	X	135800	5.05
242	2007-03-20	59862K10	X	22600	5.08
	decision.price	execution.cost	pct.exe.cost		

239	5.97	6470	3.54
240	5.97	31060	13.04
241	5.97	125126	18.25
242	5.97	20051	17.45

Here `execution.cost` denotes the dollar cost of the trade relative to the benchmark price, and `pct.exe.cost` reflects that cost as a percent of the total executed dollar amount of the trade. The decision price for the batch is \$5.97, the prior closing price on March 13. Note that the benchmark price, `decision.price`, for each trade in this batch is \$5.97. Because the price of PGIC was falling over this time period, later trades in the batch are more than five times more costly than the first trade relative to the decision price.

## Plotting results

The **tradeCosts** package includes a plot method that displays bar charts of trade costs. It requires two arguments, a `tradeCostsResults` object, and a character string that describes the type of plot to create.

The simplest plot, `time.series.bps` is a time series of total trade costs in basis points over each period:

```
> plot(result.batched, "time.series.bps")
```

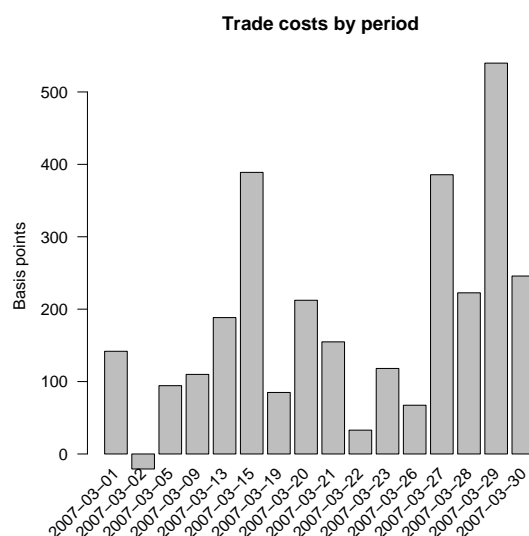


Figure 1: A time series plot of trade costs.

This chart displays the cost for each day in the previous example. According to this chart, all days had positive cost except March 2.

The second plot displays trade costs divided into categories defined by a column in the static data frame passed to `trade.costs`. Since `sector` was a column of that data frame, we can look at costs by company sector:

```
> plot(result.batched, "sector")
```

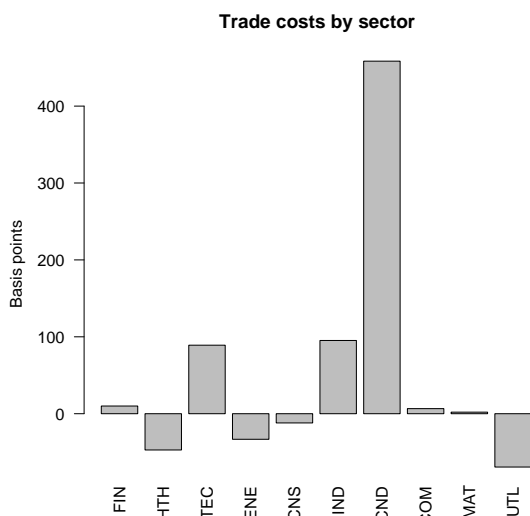


Figure 2: A plot of trade costs by sector.

Over the period of the analysis, trades in CND were especially expensive relative to decision price.

The last plot applies only to same.sided batched trade cost analysis as we performed in the multi-period example. This chart shows cost separated into the different periods of a batch. The cost of the first batch of PGIC, for example, contributes to the first bar, the cost of the second batch to the second bar, and so on.

```
> plot(result.batched, "cumulative")
```

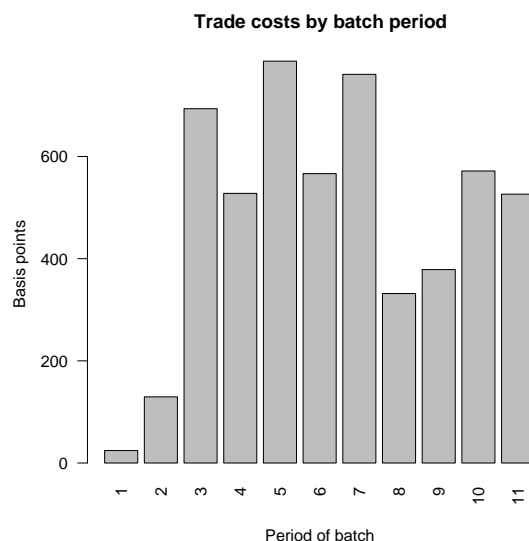


Figure 3: Costs by batch period, in bps.

As one might expect, the first and second trades in a batch are the cheapest with respect to decision price because they occur closest to the time of the decision.

## Conclusion

**tradeCosts** currently provides a simple means of calculating the cost of trades relative to a benchmark price over multiple periods. Costs may be calculated relative to a period-specific benchmark price or, for trades spanning multiple periods, the initial decision price of the trade. We hope that over time and through collaboration the package will be able to tackle more complex issues, such as ex-ante modeling and finer compartmentalization of trade costs.

## Bibliography

R. Kissell and M. Glantz. *Optimal Trading Strategies*. American Management Association, 2003.

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